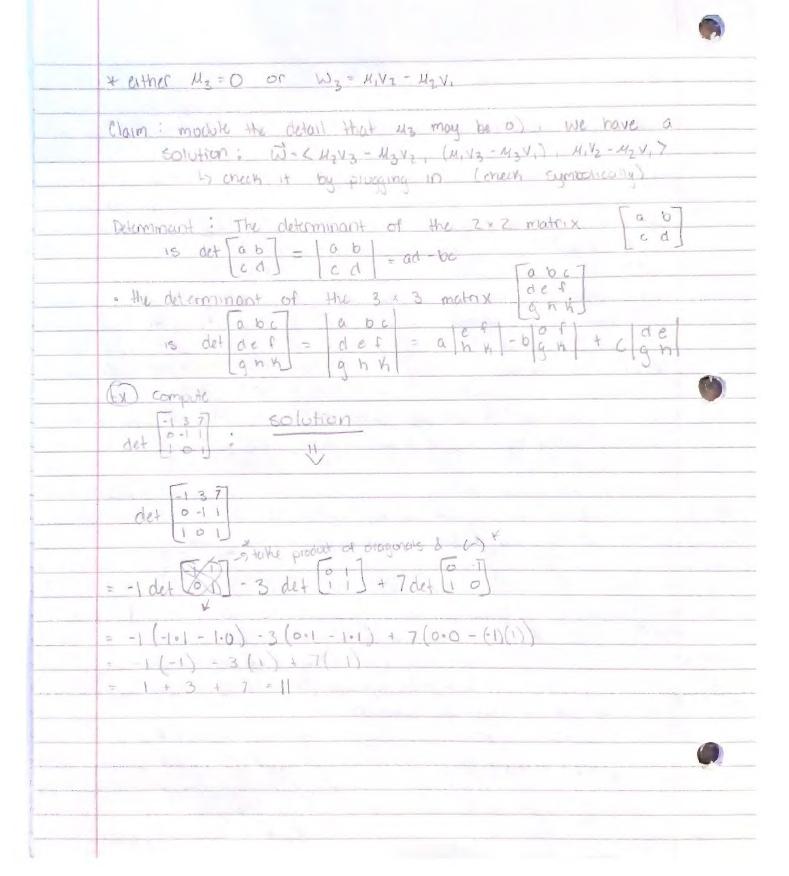
hecap: Dot product · it and it are arthogonal iff it it = 0 · the plane 5 12.4 : Cross Product Good: given two vectors. 4 = < H, H2, H3 > & V= < V, V2, V3> construct a vector  $\vec{w} = \langle w_1, w_2, w_3 \rangle \leftarrow 18^3$ that is orthogonal to both if How? We know of a - 21. D- N, W, + NZW, + U3W3 @ 0: V.W = V,W, + V2W2 + 13W3 I what ever rector we find will spitisfy this condition ( we want to compute < W, W, W, W, I's) = is Trouble el mination & · mult. 10 by V2 & 10 by 1/2 to get: Asida (0 = 43 (M, W) = (M, V3) W, + (M2 V3) W2 + (M3 V3) W3 let i X = b 0 = H3 (V.W) = (H3V,)W, + (H3V2) W2 + (H3V3) W3 ) 50 w y=a Subtract (D) from (D) V ( L. V. ( 10 - 42 ( 1. 1) والمساؤلون 0 = (H, V3 - MgV, ) W, + (M2 V2 - M3 V2) W2 = - (- (M, V3 - M3V,) W, + (M2 V2 - M3 V2) W2 @ has at least the solution W. - H2V3 - H3V2 > 0= 4, W, + 4, W, + H2 W2 Wz = - (1/1/3 - 1/3 /) = M, (M2 V3 - M3 V2) + M2 (-(M, V3 - M2 V, ) + 1/2 W, = M, M2 43 - M, M3 V2 - M, M3 V2 + M2 M3 V, + Mh · inputting these to 0 we obtain: = M3 (My V1 - M1/2 + W3)



777 Defn: Let #= < 4, 42, 437, V- (u, v2, U3) & 1R3 19 the cross product of  $\vec{A}$  with  $\vec{v}$  is:  $\vec{A} \cdot \vec{V} = \begin{vmatrix} \vec{A} & \vec{A} & \vec{A} \\ \vec{A} & \vec{A} & \vec{A} \end{vmatrix}$ TI. = (M2 V2 - M2 V2) = - (M, V3 - M3 V, ) + + (M, V2 - M2 V, ) & 1/2 = < 11213-113V2, (1, V3-113V,), 11, V2-112V,) Lange & CROSS FRODUCT of this has to be done in 123, much more would needed to do in 124 (including more vectors · the cross product is a vector operation ( Vector in R3 X vector in R3 - 3 vector in R3 comil coumples undefined 1 is not a vector 2 5 undefined not in Proposition ( Algebraic properties of cross product ): M. V. DER3 and GEB econtrol commonline \* it (showing it the opp. way but some idea) = (Valla - Valla): - (Valla - Valla) + (Valla - Valla) + = < V, M3 - V3 M2 - (V, M3 - V3 M, ) , V, M2 - V2 M, ) -- ( V3M2 - 43 V2 , - (N, V3 - M3V.) , AI, V2 - M2V.) - - DI = 7

(3)	$(C\vec{a}) \times \vec{v} = C(\vec{a} \times \vec{v}) = \vec{a} \times (C\vec{v})$
(3)	$\vec{\mu} \times (\vec{v} + \vec{\omega}) = (\vec{\mu} \times \vec{v}) + (\vec{\mu} \times \vec{\omega}) : distribution on left$
9	$(\vec{u} + \vec{v}) \times \vec{\omega} = (\vec{u} \times \vec{\omega}) + (\vec{v} \times \vec{\omega}) : distribution on right$
	$\vec{\eta} \cdot (\vec{y} \times \vec{\omega}) = (\vec{u} \times \vec{y}) \cdot \vec{\omega} + \text{not associative bis is a diff.}$
0	$\vec{H} \times (\vec{v} \times \vec{\omega}) = (\vec{\mu} \cdot \vec{\omega}) \vec{v} - (\vec{\mu} \cdot \vec{v}) \vec{\omega}$ * NOT Associative : () (and shift
	Properties (Geometric of cross product): -Let il, v E 13
d	Il x v is orthogonal to both il 8 v
Œ)	$ \vec{u} \times \vec{v}  =  \vec{u}  \vec{v}  _{SM} \theta  \text{w/}  \theta  \text{the ongle between } \vec{u}  s  \vec{v}$
3	$\vec{\mu} \times \vec{v} = \vec{o}$ iff $\vec{n} = \vec{v}$ (parallel)